# SbSb<sub>x</sub> $M_{1-x}O_4$ ( $M = Nb^{\vee}$ or Ta<sup> $\vee$ </sup>): Solid Solution Behavior and Second-Harmonic Generating Properties

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The solid solution behavior and second-harmonic generating (SHG) properties of  $SbSb_xM_{1-x}O_4$  ( $M = Nb^V$  or  $Ta^V$ ) (x = 0.0, 0.2, 0.4, 0.5, 0.6, 0.8, and 1.0) have been investigated by powder X-ray diffraction and nonlinear optical (NLO) measurements. Both  $SbNbO_4$  and  $SbTaO_4$  form solid solutions with  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>. All the materials crystallize in the non-centrosymmetric space group  $Pna2_1$ , with  $Sb^{III}O_4E$  polyhedra linked to  $M^VO_6$  ( $M^V = Sb^V$ ,  $Nb^V$ , or  $Ta^V$ ) octahedra. SHG data is presented for the solid solutions and  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>, SbNbO<sub>4</sub>, and SbTaO<sub>4</sub>. With respect to the  $SbSb_xM_{1-x}O_4$  phases, NLO measurements indicate a substantial decrease in SHG efficiency for  $x \ge 0.6$ . This decrease is attributable to the "nonpolar" nature of  $Nb^VO_6$  or  $Ta^VO_6$ . © 2001 Academic Press

*Key Words:* oxides; solid solution; second-harmonic generation; powder X-ray diffraction.

## **INTRODUCTION**

The elucidation of structure-property relationships remains an ongoing challenge in solid-state materials chemistry. This is particularly true for second-order nonlinear optical (NLO), i.e., second-harmonic generating (SHG), materials (1-5). Viable SHG materials should possess the following attributes: chemical stability, transparency in the relevant wavelengths, and the ability to withstand laser irradiation, but most importantly the material must be crystallographically non-centrosymmetric (NCS) (6). In a review of NCS oxides (3), we determined the influence of a second-order Jahn-Teller (SOJT) distortion (7-13) on the acentric structure. In addition, we recently reported the syntheses, structures, and SHG behavior of some compounds that contain SOJT distorted cations (14-16). Through the powder SHG measurements we were able to estimate  $\langle d_{ijk}^{2\omega} \rangle$ , the average NLO bond susceptibility. One of the aims of our research is not only to synthesize SHG

materials but also to understand the structural origin of the NLO phenomenon. With this in mind, we investigated the α-Sb<sub>2</sub>O<sub>4</sub> (17, 18), SbNbO<sub>4</sub>, and SbTaO<sub>4</sub> (19, 20) oxides. These compounds represent an isostructural oxide series, crystallizing in the NCS space group Pna21. The materials consist of  $Sb^{III}O_4E$  polyhedra, where E is the nonbonded electron pair, and  $MO_6$  octahedra ( $M = Sb^V$ ,  $Nb^V$ , or  $Ta^V$ ). With respect to connectivity, the structures can be described as  $[SbO_{4/3}]^{1/3+}$  cations linked to  $[MO_{4/2}O_{2/3}]^{1/3-}$  anions. A representation of the structure is given in Fig. 1. Both SbNbO<sub>4</sub> and SbTaO<sub>4</sub> are SHG active and ferroelectric with Curie temperatures of 605 and 600°C, respectively (21). The solid solution behavior of  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>-SbNbO<sub>4</sub> and  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>-SbTaO<sub>4</sub> has been briefly discussed (22), but a detailed study was not carried out. In this paper we describe the synthesis and SHG behavior of the  $SbSb_xNb_{1-x}O_4$  and  $SbSb_xTa_{1-x}O_4$  solid solutions. In addition, we describe in detail the SHG behavior of a-Sb<sub>2</sub>O<sub>4</sub>, SbNbO<sub>4</sub>, and SbTaO<sub>4</sub>, including an estimate of a specific NLO bond susceptibility tensor,  $d_{333}$ , for SbNbO<sub>4</sub> and SbTaO<sub>4</sub>.

## EXPERIMENTAL

Synthesis. The SbSb<sub>x</sub> $M_{1-x}O_4$  (M = Nb or Ta; x = 0.2, 0.4, 0.5, 0.6, 0.8) phases were synthesized through standard solid-state techniques. Stoichiometric amounts of Sb<sub>2</sub>O<sub>3</sub> (Alfa, 99.6%) with either Nb<sub>2</sub>O<sub>5</sub> (Aldrich, 99.99%) or Ta<sub>2</sub>O<sub>5</sub> (Aldrich, 99%) and Sb<sub>2</sub>O<sub>5</sub> (Aldrich, 99.995%) were thoroughly ground with an agate mortar and pestle and pressed into pellets. The pellets were wrapped with platinum foil and introduced into a quartz tube that was sealed under vacuum. Each tube was heated to 550°C for 3 h and then to 650°C (800°C for SbSb<sub>x</sub>Ta<sub>1-x</sub>O<sub>4</sub> phases) for 48 h. The samples were cooled at a rate of 10°C/min to room temperature. Polycrystalline  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub> was synthesized by heating Sb<sub>2</sub>O<sub>3</sub> in air at 600°C for 24 h. SbNbO<sub>4</sub> and SbTaO<sub>4</sub> were prepared as previously reported (23, 24).

Diffraction and crystal structure refinement. The X-ray powder diffraction data were collected on a Scintag



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**FIG. 1.** Ball-and-stick representation of  $SbMO_4$  ( $M = Sb^{V}$ ,  $Nb^{V}$ , or  $Ta^{V}$ ).

XDS2000 diffractometer at room temperature (CuKα radiation,  $\theta - \theta$  mode, flat plate geometry) in the  $2\theta$  range  $3^{\circ} - 110^{\circ}$ with a step size of  $0.02^{\circ}$  and a step time of 10s. The diffraction patterns were analyzed using the Rietveld method (25) with the FULLPROF program (26). The peaks were indexed on an orthorhombic cell, with refinement of the unit-cell constants for  $SbSb_xM_{1-x}O_4$  (M = Nb or Ta; x = 0.2, 0.4, 0.5, 0.6, 0.8) performed using a least-squares method (see Table 1). The structural refinements of  $SbSb_{0.5}M_{0.5}O_4$  (M = Nb or Ta) were carried out in the space group  $Pna2_1$  (No. 33) with a starting model similar to SbNbO<sub>4</sub> (19). A total of 33 parameters, including 11 profile parameters, were used during the refinements. An asymmetry correction was applied to the low-angle reflections. The scale was refined initially, followed in subsequent iterations by the zero point error, cell constants, peak shape parameters, atomic parameters, and overall isotropic temperature factors. The results of the refinements are summarized in Table 2, with atomic positions and isotropic thermal parameters given in Table 3.

Second-order nonlinear optical measurements. Powder SHG measurements were performed on a modified Kurtz–NLO (27) system using 1064-nm light. A Continuum Minilite II laser, operating at 15 Hz, was used for all measurements. The average energy per pulse was 3 mJ. Since the SHG efficiency of powders has been shown to depend strongly on particle size (27, 28), polycrystalline  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>, SbNbO<sub>4</sub>, and SbTaO<sub>4</sub> were ground and sieved (Newark Wire Cloth Co.) into distinct particle size ranges: < 20 µm, 20–45 µm, 45–63 µm, 63–75 µm, 75–90 µm, and 90–125 µm. For the compounds in the solid solution, the

TABLE 1Unit Cell Constants for  $Sb(Sb_xM_{1-x})O_4$  (M = Nb or Ta)

Compound	a (Å)	b (Å)	c (Å)	$V(\text{\AA}^3)$
SbNbO <sub>4</sub>	5.5630(3)	4.9305(3)	11.8038(6)	323.76(3)
Sb(Sb <sub>0.2</sub> Nb <sub>0.8</sub> )O <sub>4</sub>	5.5458(2)	4.9095(1)	11.8009(3)	321.30(4)
$Sb(Sb_{0,4}Nb_{0,6})O_4$	5.5241(2)	4.8866(2)	11.7982(5)	318.48(5)
$Sb(Sb_{0.5}Nb_{0.5})O_4$	5.5140(2)	4.8761(2)	11.7961(5)	317.16(5)
Sb(Sb <sub>0.6</sub> Nb <sub>0.4</sub> )O <sub>4</sub>	5.4982(2)	4.8638(2)	11.7916(5)	315.33(5)
Sb(Sb <sub>0.8</sub> Nb <sub>0.2</sub> )O <sub>4</sub>	5.4733(4)	4.8433(3)	11.7927(8)	312.61(7)
$\alpha$ -Sb <sub>2</sub> O <sub>4</sub>	5.4429(3)	4.8084(3)	11.7810(6)	308.33(3)
Compound	(*)		( ? )	
Compound	$a(\mathbf{A})$	<i>b</i> (A)	<i>c</i> (A)	$V(\mathbf{A}^{3})$
SbTaO <sub>4</sub>	a (A) 5.5361(9)	b (A) 4.9117(3)	c (A)	V (A <sup>3</sup> ) 321.45(4)
SbTaO <sub>4</sub> Sb(Sb <sub>0.2</sub> Ta <sub>0.8</sub> )O <sub>4</sub>	a (A) 5.5361(9) 5.5258(1)	<i>b</i> (A) 4.9117(3) 4.9004(1)	c (A) 11.8215(6) 11.8125(3)	V (A <sup>3</sup> ) 321.45(4) 319.87(4)
SbTaO <sub>4</sub> Sb(Sb <sub>0.2</sub> Ta <sub>0.8</sub> )O <sub>4</sub> Sb(Sb <sub>0.4</sub> Ta <sub>0.6</sub> )O <sub>4</sub>	a (A) 5.5361(9) 5.5258(1) 5.5090(1)	<i>b</i> (A) 4.9117(3) 4.9004(1) 4.8836(1)	c (A) 11.8215(6) 11.8125(3) 11.8057(3)	V (A <sup>3</sup> ) 321.45(4) 319.87(4) 317.62(4)
SbTaO <sub>4</sub> Sb(Sb <sub>0.2</sub> Ta <sub>0.8</sub> )O <sub>4</sub> Sb(Sb <sub>0.4</sub> Ta <sub>0.6</sub> )O <sub>4</sub> Sb(Sb <sub>0.5</sub> Ta <sub>0.5</sub> )O <sub>4</sub>	a (A) 5.5361(9) 5.5258(1) 5.5090(1) 5.5019(2)	<i>b</i> (A) 4.9117(3) 4.9004(1) 4.8836(1) 4.8762(2)	c (A) 11.8215(6) 11.8125(3) 11.8057(3) 11.8038(4)	V (A <sup>3</sup> ) 321.45(4) 319.87(4) 317.62(4) 316.68(5)
SbTaO <sub>4</sub> Sb(Sb <sub>0.2</sub> Ta <sub>0.8</sub> )O <sub>4</sub> Sb(Sb <sub>0.4</sub> Ta <sub>0.6</sub> )O <sub>4</sub> Sb(Sb <sub>0.5</sub> Ta <sub>0.5</sub> )O <sub>4</sub> Sb(Sb <sub>0.5</sub> Ta <sub>0.5</sub> )O <sub>4</sub>	a (A) 5.5361(9) 5.5258(1) 5.5090(1) 5.5019(2) 5.4922(2)	<i>b</i> (A) 4.9117(3) 4.9004(1) 4.8836(1) 4.8762(2) 4.8646(2)	c (A) 11.8215(6) 11.8125(3) 11.8057(3) 11.8038(4) 11.7988(4)	V (A <sup>3</sup> ) 321.45(4) 319.87(4) 317.62(4) 316.68(5) 315.23(5)
$\frac{\text{SbTaO}_{4}}{\text{Sb}(\text{Sb}_{0.2}\text{Ta}_{0.8})\text{O}_{4}}$ $\frac{\text{Sb}(\text{Sb}_{0.4}\text{Ta}_{0.6})\text{O}_{4}}{\text{Sb}(\text{Sb}_{0.5}\text{Ta}_{0.5})\text{O}_{4}}$ $\frac{\text{Sb}(\text{Sb}_{0.5}\text{Ta}_{0.4})\text{O}_{4}}{\text{Sb}(\text{Sb}_{0.6}\text{Ta}_{0.4})\text{O}_{4}}$	a (A) 5.5361(9) 5.5258(1) 5.5090(1) 5.5019(2) 5.4922(2) 5.4680(2)	b (A) 4.9117(3) 4.9004(1) 4.8836(1) 4.8762(2) 4.8646(2) 4.8380(2)	c (A) 11.8215(6) 11.8125(3) 11.8057(3) 11.8038(4) 11.7988(4) 11.7705(5)	V (A <sup>3</sup> ) 321.45(4) 319.87(4) 317.62(4) 316.68(5) 315.23(5) 311.38(5)
$\begin{array}{c} \mbox{SbTaO}_4 \\ \mbox{Sb(Sb}_{0.2} Ta_{0.8}) O_4 \\ \mbox{Sb(Sb}_{0.4} Ta_{0.6}) O_4 \\ \mbox{Sb(Sb}_{0.5} Ta_{0.5}) O_4 \\ \mbox{Sb(Sb}_{0.6} Ta_{0.4}) O_4 \\ \mbox{Sb(Sb}_{0.8} Ta_{0.2}) O_4 \\ \mbox{Sb(Sb}_{0.8} Ta_{0.2}) O_4 \\ \mbox{\alpha-Sb}_2 O_4 \end{array}$	a (A) 5.5361(9) 5.5258(1) 5.5090(1) 5.5019(2) 5.4922(2) 5.4680(2) 5.4429(3)	b (A) 4.9117(3) 4.9004(1) 4.8836(1) 4.8762(2) 4.8646(2) 4.8380(2) 4.8084(3)	c (A) 11.8215(6) 11.8125(3) 11.8057(3) 11.8038(4) 11.7988(4) 11.7705(5) 11.7810(6)	V (A <sup>3</sup> ) 321.45(4) 319.87(4) 317.62(4) 316.68(5) 315.23(5) 311.38(5) 308.33(3)

powders in the 45–63  $\mu$ m were used for SHG intensity measurements. To make relevant comparisons with known SHG materials, crystalline SiO<sub>2</sub> was also ground and sieved into the same particle size ranges. All the powders were placed in separate capillary tubes. The SHG, i.e., 532 nm green light, radiation was collected in reflection and detected by a photomultiplier tube (Oriel Instruments). To detect only the SHG light, a 532nm narrow-bandpass interference filter was attached to the tube. A digital oscilloscope (Tektronix TDS 3032) was used to view the SHG signal.

 TABLE 2

 Summary of Crystallographic Data and Refinement Results

 for Sb(Sb<sub>0.5</sub> $M_{0.5}$ )O<sub>4</sub> (M = Nb or Ta)

Compound	$Sb(Sb_{0.5}Nb_{0.5})O_4$	$Sb(Sb_{0.5}Ta_{0.5})O_4$
a (Å)	5.5140(2)	5.5019(2)
b (Å)	4.8761(2)	4.8762(2)
<i>c</i> (Å)	11.7961(5)	11.8038(4)
$V(Å^3)$	317.16(5)	316.68(5)
Space group	<i>Pna</i> 2 <sub>1</sub> (No. 33)	<i>Pna</i> 2 <sub>1</sub> (No. 33)
Observations	413	412
$\chi^2$	2.30	2.24
$R_{p}^{a}$	0.116	0.163
$\hat{R_{wp}}^{b}$	0.152	0.181
$R_{exp}^{c}$	0.101	0.121
$R_{\text{Bragg}}^{d}$	0.046	0.064

Note.  $I_o$  and  $I_c$  are the observed and calculated integrated intensities,  $I_k$  is the Bragg intensity, and w is the weight derived from an error propagation scheme during the process of least-squares refinement.

<sup>*a*</sup> 
$$R_{\rm p} = \sum |I_{\rm o} - I_{\rm c}| / \sum I_{\rm o}.$$
  
<sup>*b*</sup>  $R_{\rm wp} = [\sum w |I_{\rm o} - I_{\rm c}|^2 / \sum w I_{\rm o}^2]^{1/2}.$ 

$$K_{wp} = \sum W |I_0 - I_c|^2$$

$$\kappa_{\rm exp} = \kappa_{\rm wp} / (\chi)^{-1} .$$

<sup>d</sup>  $R_{\text{Bragg}} = \sum |I_{k(\text{obs})} - I_{k(\text{calc})}| / \sum I_{k(\text{obs})}$ 

TABLE 3Fractional Atomic Coordinates, Isotropic Temperature Factors $(Å^2)$ , and Occupancies for Sb $(Sb_{0.5}M_{0.5})O_4$  (M = Nb or Ta)

Atom	x	У	Ζ	$B_{\rm iso}$	Occupancy
		Sb(Sb <sub>0.5</sub>	$Nb_{0.5}O_4$		
Nb/Sb(1)	0.1194(6)	-0.006(2)	-0.071(1)	1.7(1)	$0.5/0.5^{a}$
Sb(2)	0.478(1)	0.043(6)	0.178(2)	2.1(1)	1.0
O(1)	0.183(6)	-0.149(6)	-0.226(3)	$0.8(3)^{b}$	1.0
O(2)	0.420(6)	-0.188(6)	-0.008(3)	$0.8(3)^{b}$	1.0
O(3)	0.146(6)	0.182(6)	0.087(3)	$0.8(3)^{b}$	1.0
O(4)	0.363(6)	0.281(6)	- 0.123(3)	$0.8(3)^{b}$	1.0
		Sb(Sb <sub>0.5</sub>	$Ta_{0.5}O_4$		
Ta/Sb(1)	0.1249(6)	-0.005(3)	-0.138(1)	2.2(1)	$0.5/0.5^{a}$
Sb(2)	0.479(2)	0.045(1)	0.112(2)	3.0(2)	1.0
O(1)	0.154(9)	-0.116(9)	-0.327(3)	$0.3(6)^{c}$	1.0
O(2)	0.353(9)	-0.289(9)	-0.084(3)	$0.3(6)^{c}$	1.0
O(3)	0.159(9)	0.186(9)	-0.002(3)	$0.3(6)^{c}$	1.0
O(4)	0.424(9)	0.185(9)	- 0.188(3)	$0.3(6)^{c}$	1.0

<sup>*a*</sup> Statistically disordered with 50% Sb<sup>v</sup> and 50%  $M^{v}$  ( $M = Nb^{v}$  or Ta<sup>v</sup>). Atomic coordinates constrained to be equal.

<sup>b, c</sup> Thermal parameters constrained to be equal.

### **RESULTS AND DISCUSSION**

Both SbNbO<sub>4</sub> and SbTaO<sub>4</sub> form solid solutions with  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>. The powder X-ray diffraction data for both solid solutions are shown in Figs. 2a and 2b, with the refined unit cell for each compound given in Table 1. As expected, the cell volume decreases with increasing Sb<sup>v</sup> on the Nb<sup>v</sup> or Ta<sup>V</sup> site. The volume change is less for the  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>-SbTaO<sub>4</sub> solid solution than for  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>-SbNbO<sub>4</sub>. This is attributable to the similar size of six-coordinate Sb<sup>V</sup> (0.60 Å) compared with that of six-coordinate Ta<sup>v</sup> (0.64 Å), which is smaller than six-coordinate Nb<sup>V</sup> (0.68 Å) (29). However, the unit cell changes are anisotropic, with the changes in a and b around 2%, whereas the change in c is only  $\sim 0.25\%$ . This anisotropic change in unit cell is consistent with the loss of polarization in changing from a  $M^{V}O_{6}$  octahedra to Sb<sup>V</sup>O<sub>6</sub> octahedra (vide infra). We were able to refine the structures for SbSb<sub>0.5</sub>Nb<sub>0.5</sub>O<sub>4</sub> and SbSb<sub>0.5</sub>Ta<sub>0.5</sub>O<sub>4</sub> (see Table 2 and auxiliary material).<sup>2</sup> We did not observe any ordering between Sb<sup>V</sup> and  $M^V$  ( $M = Nb^V$  or Ta<sup>V</sup>) throughout the range of the solid solutions.

The SHG behaviour of the  $\text{SbSb}_x M_{1-x} O_4$  ( $M = \text{Nb}^{V}$  or  $\text{Ta}^{V}$ ) solid solutions is shown in Figs. 3a and 3b. For both solid solutions the SHG efficiency decreases markedly for  $x \ge 0.6$ , i.e.,  $\text{SbSb}_{0.6} M_{0.4} O_4$ , and for pure  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub> the SHG is only slightly more efficient than SiO<sub>2</sub>. This would strongly

<sup>&</sup>lt;sup>2</sup> Experimental and calculated powder X-ray diffraction data and difference plots for SbSb<sub>0.5</sub>Nb<sub>0.5</sub>O<sub>4</sub>, SbSb<sub>0.5</sub>Ta<sub>0.5</sub>O<sub>4</sub> and indexed powder X-ray diffraction data for SbSb<sub>x</sub> $M_{1-x}$ O<sub>4</sub> (M =Nb<sup>v</sup> or Ta<sup>v</sup>) for x = 0.0, 0.2, 0.4, 0.6, 0.8, and 1.0 are available from the author upon request.



FIG. 2. Powder X-ray diffraction data for (a)  $SbSb_xNb_{1-x}O_4$  and (b)  $SbSb_xTa_{1-x}O_4$ .



**FIG. 3.** SHG vs Sb<sup>V</sup> doping in (a) SbSb<sub>x</sub>Nb<sub>1-x</sub>O<sub>4</sub> and (b) SbSb<sub>x</sub>Ta<sub>1-x</sub>O<sub>4</sub>. In both figures, note the marked decrease in SHG efficiency for  $x \ge 0.6$ 

suggest that the structural origin of the SHG is attributable to the distorted  $MO_6$  ( $M = Nb^V$  or  $Ta^V$ ) octahedra and not the  $Sb^{III}O_4E$  group, even though both cations,  $M^V$  and  $Sb^{III}$ , are in asymmetric coordination environments. The reduction in SHG is consistent with the net polarization of the respective metal polyhedra. The Sb<sup>III</sup> cation, in SbMO<sub>4</sub>, is in an asymmetric coordination environment attributable to the nonbonded electron pair. The cation is bonded to four oxygen atoms in a distorted square pyramidal geometry. In the SbMO<sub>4</sub> structure, the polarization on the Sb<sup>III</sup>O<sub>4</sub>E group alternates between the [010] and  $[0\overline{1}0]$  directions. Thus, the net polarization, i.e., dipole moment, associated with Sb<sup>III</sup> in NCS Sb $MO_4$  is zero. The  $M^V$  cations ( $M = Nb^V$  or  $Ta^V$ ) are also in a distorted coordination environment. Here, the cation is intraoctahedrally distorted, resulting in two "short" and four "long" bonds to oxygen. When the  $M^{V}$ octahedra are taken in their entirely, a net polarization, i.e., dipole moment, is observed along the [011] direction. Thus, from a structural approximation the SHG efficiency is at-



FIG. 4. Phase matching, i.e., particle size vs SHG intensity, data for  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>. The curve is drawn to guide the eye and is not a fit to the data.

tributable to this  $M^{V}$  polarization. When Sb<sup>V</sup> is substituted for this "polarized" cation, the SHG efficiency decreases. This decrease is attributable to the isotropic environment of Sb<sup>V</sup>, i.e., no dipole moment in the Sb<sup>V</sup>O<sub>6</sub> octahedra. Thus, similar to replacing Ti<sup>IV</sup> with Sn<sup>IV</sup> in KTiOPO<sub>4</sub> (KTP) (30), the inclusion of a nonpolarizable cation, in our case Sb<sup>V</sup>, is detrimental to the SHG efficiency.

As previously stated, the single-crystal NLO behavior of SbNbO<sub>4</sub> and SbTaO<sub>4</sub> has been studied (21, 31). We investigated the powder SHG behavior for  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>, SbNbO<sub>4</sub>, and SbTaO<sub>4</sub> and determined that none of the materials are phase matchable (see Figs. 4, 5, and 6). We also determined that the compounds have SHG efficiencies of 10, 400, and 350 times SiO<sub>2</sub>, respectively. Previous SHG measurements on single-crystals SbMO<sub>4</sub> ( $M = Nb^{V}$  or Ta<sup>V</sup>) enabled the



**FIG. 5.** Phase matching, i.e., particle size vs SHG intensity, data for SbNbO<sub>4</sub>. The curve is drawn to guide the eye and is not a fit to the data.



**FIG. 6.** Phase matching, i.e., particle size vs SHG intensity, data for SbTaO<sub>4</sub>. The curve is drawn to guide the eye and is not a fit to the data.

researchers to deduce the specific  $\langle d_{ijk}^{2\omega} \rangle$ , NLO bond susceptibility, values. SbNbO<sub>4</sub> and SbTaO<sub>4</sub> crystallize in the orthorhombic space group *Pna*2<sub>1</sub>, which is in point group *mm*2. Point group *mm*2 has three independent SHG modulii, assuming Kleinman symmetry is valid (32);  $d_{311} = d_{113}$ ,  $d_{322} = d_{223}$ , and  $d_{333}$ . In their original paper, Kurtz and Perry deduced that for unpolarized fundamental and second-harmonic light (27)

$$\begin{aligned} (\langle d_{ijk}^{2\omega} \rangle)^2 &= (19/105) \sum_i (d_{iii})^2 + (13/105) \sum_{i \neq j} (d_{iii})(d_{ijj}) \\ &+ (44/105) \sum_{i \neq j} (d_{iij})^2 + (13/105) \sum_{ijk, \text{ cyclic}} (d_{iij})(d_{jkk}) \\ &+ (5/7) (d_{ijk})^2. \end{aligned}$$

For point group, i.e., crystal class, mm2, Eq. [1] reduces to

$$\langle d_{ijk}^{200} \rangle^2 = (19/105)(d_{333})^2 + (26/105)(d_{333})(d_{311}) + (44/105)(d_{113})^2 + (44/105)(d_{223})^2 + (26/105)(d_{113})(d_{223}).$$
[2]

For SbNbO<sub>4</sub>,  $d_{311} = 5.90 \text{ pm/V}$  and  $d_{223} = 5.75 \text{ pm/V}$  (21, 31). Putting these values into Eq. [2],

$$\{(\langle d_{ijk}^{2\omega} \rangle)^2 \text{ (SbNbO}_4)\} = (0.18)(d_{333})^2 + 1.46 \text{ pm/V} (d_{333}) + 36.9 \text{ pm}^2/\text{V}^2.$$
[3]

For two non-phase-matchable materials, the intensity ratio can be written (27)

$$I^{2\omega} (\text{SbNbO}_4)/I^{2\omega} (\text{SiO}_2) = \left[ (\langle d_{ijk}^{2\omega} \rangle)^2 \times \frac{(l_c)^2}{2r} \right] (\text{SbNbO}_4) / \left[ (\langle d_{ijk}^{2\omega} \rangle^2) \times \frac{(l_c)^2}{2r} \right] (\text{SiO}_2).$$
[4]

TABLE 4Summary of SHG Data

Compound	$I^{2\omega}/I^{2\omega}$ (SiO <sub>2</sub> )	$\langle d^{2\omega}_{ijk}  angle$
SiO <sub>2</sub>	1	0.28 pm/V <sup>a</sup>
$\alpha$ -Sb <sub>2</sub> O <sub>4</sub>	10	$1.8 \text{ pm/V}^b$
SbNbO <sub>4</sub>	400	$11.0 \text{ pm/V}^b$
SbTaO <sub>4</sub>	350	$10.1 \text{ pm}/\text{V}^{b}$
SbSb <sub>0.5</sub> Nb <sub>0.5</sub> O <sub>4</sub>	375	$10.7 \text{ pm}/\text{V}^{b}$
$SbSb_{0.5}Ta_{0.5}O_4$	300	9.6 pm/V <sup>b</sup>
Appro	ximate NLO bond suscept	tibilities
$d_{333}$ (SbNbO <sub>4</sub> )	18 pm/V <sup>b</sup>	
$d_{222}$ (SbTaO <sub>4</sub> )	$17 \text{ pm/V}^{b}$	

<sup>*a*</sup> Calculated from reported single-crystal NLO data. <sup>*b*</sup> This work.

The coherence length,  $l_c$ , is 20 µm for SiO<sub>2</sub> and is assumed to be 10 µm for SbNbO<sub>4</sub>, whereas the average particle size, *r*, is taken to be 50 µm for both materials (27). The value of  $\{(\langle d_{ijk}^{2\omega} \rangle)^2 (SiO_2)\}$  can be calculated from single-crystal data and is equal to  $7.62 \times 10^{-2} \text{ pm}^2/\text{V}^2$ . SbNbO<sub>4</sub> has an SHG intensity of 400 times SiO<sub>2</sub>. Setting Eq. [4] equal to 400 and solving for  $\{(\langle d_{ijk}^{2\omega} \rangle)^2 (\text{SbNbO}_4)\}$  results in a value of  $1.22 \times 10^2 \text{ pm}^2/\text{V}^2$ . Therefore, Eq. [3] becomes

$$1.22 \times 10^2 \text{ pm}^2/\text{V}^2 = (0.18) (d_{333})^2 + 1.46 \text{ pm}/\text{V} (d_{333})$$
  
+ 36.9 pm<sup>2</sup>/V<sup>2</sup>. [5]

Solving Eq. [5] for  $d_{333}$  results in a value of approximately 18 pm/V. Repeating the procedure for SbTaO<sub>4</sub>, which has a SHG efficiency of 350 times SiO<sub>2</sub> with  $d_{311} = 5.10 \text{ pm/V}$  and  $d_{223} = 5.00 \text{ pm/V}$  (21, 31), results in a { $(\langle d_{ijk}^{2\omega} \rangle)^2$  (SbTaO<sub>4</sub>)} value of  $1.07 \times 10^{-2} \text{ pm}^2/\text{V}^2$ . Thus,  $d_{333}$  for SbTaO<sub>4</sub> is approximately 17 pm/V.

Based only on powder SHG data, we may calculate the average bond susceptibility value,  $\langle d_{ijk}^{2\omega} \rangle$ , for  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>, SbSb<sub>0.5</sub>Nb<sub>0.5</sub>O<sub>4</sub>, and SbSb<sub>0.5</sub>Ta<sub>0.5</sub>O<sub>4</sub>. These materials have a SHG efficiency of 10, 375, and 300 times SiO<sub>2</sub>. Also all the materials are not phase matchable. Equation [4] describes the intensity ratio for two non-phase-matchable materials. This equation may be solved for  $\langle d_{ijk}^{2\omega} \rangle$  for  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>, SbSb<sub>0.5</sub>Nb<sub>0.5</sub>O<sub>4</sub>, and SbSb<sub>0.5</sub>Ta<sub>0.5</sub>O<sub>4</sub>, respectively, by setting Eq. [4] equal to 10, 375, and 300 and using the same values for  $l_c$  and r as before. Doing so results in values of 1.8, 10.7, and 9.6 pm/V for  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>, SbSb<sub>0.5</sub>Nb<sub>0.5</sub>O<sub>4</sub>, respectively. These values are the *average* NLO bond susceptibilities, for the entire material, and not for specific susceptibility tensors. Table 4 summarizes the SHG data described in this paper.

#### CONCLUSION

The solid solution and powder SHG behavior of  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>-SbNbO<sub>4</sub> and  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>-SbTaO<sub>4</sub> has been

investigated. We determined that both SbNbO<sub>4</sub> and SbTaO<sub>4</sub> form solid solutions with  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>. We also determined that the SHG efficiency decreases markedly in SbSb<sub>x</sub>M<sub>1-x</sub>O<sub>4</sub> ( $M = Nb^{V}$  or Ta<sup>V</sup>) for  $x \ge 0.6$ . The decrease in SHG upon the addition of Sb<sup>V</sup> strongly suggests that the structural origin for the SHG is attributable to the distorted  $M^{V}O_{6}$  octahedra and not the Sb<sup>III</sup>O<sub>4</sub>E group. This is consistent with the observation that the SHG efficiency of SbNbO<sub>4</sub> and SbTaO<sub>4</sub> are substantially greater than  $\alpha$ -Sb<sub>2</sub>O<sub>4</sub>. We are in the process of investigating other SHG materials and will be reporting on them shortly.

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